

Preprint of the paper which appeared in:  
Robotics and Autonomous Systems 119 (2019) 185–200  
<https://doi.org/10.1016/j.robot.2019.06.009>

## An Introductory Review of Active Compliant Control

Marie Schumacher<sup>a,\*</sup>, Janis Wojtusch<sup>a</sup>, Philipp Beckerle<sup>b</sup>, Oskar von Stryk<sup>a</sup>

<sup>a</sup>*Simulation, Systems Optimization, and Robotics Group, TU Darmstadt, Germany*

<sup>b</sup>*Institute for Mechatronic Systems in Mechanical Engineering, TU Darmstadt, Germany*

---

### Abstract

Active compliant control enables to quickly and freely adjust the properties and dynamic behavior of interactions of mechanisms within certain limits. According to the emerging applications in many robotic fields and related areas, the number of publications has also strongly increased. This paper meets the need for a recent comprehensive review, including a profound and concise characterization and classification of compliant control approaches extending the basic concepts, hybrid and parallel force/position, impedance and admittance control, by a survey of their variants and combinations. It mainly focuses on individually operating, stiff, non-redundant systems. Unlike previous reviews, this work is based on a transparent and systematic literature search methodology, which can easily be adapted or updated by any reader, hence remaining enduringly up-to-date over time. Also, a novel selection scheme is proposed, which facilitates the choice of appropriate control approaches for given requirements, particularly for newcomers to the field.

*Keywords:* Compliant control; Impedance control; Admittance control; Hybrid force/position control; Parallel force/position control; Force control.

---

\*Correspondence to: Technische Universität Darmstadt, Simulation, Systems Optimization, and Robotics Group, Hochschulstraße 10, 64289 Darmstadt, Germany.

*Email addresses:* [schumacher@sim.tu-darmstadt.de](mailto:schumacher@sim.tu-darmstadt.de) (Marie Schumacher), [Janis.Wojtusch@esa.int](mailto:Janis.Wojtusch@esa.int) (Janis Wojtusch), [beckerle@ims.tu-darmstadt.de](mailto:beckerle@ims.tu-darmstadt.de) (Philipp Beckerle), [stryk@sim.tu-darmstadt.de](mailto:stryk@sim.tu-darmstadt.de) (Oskar von Stryk)

## 1. Introduction

The emerging field of compliant control has evolved from hybrid to parallel force/position control and to impedance and admittance control. Compliant control is a subdomain of continuous feedback force control and allows to virtually manipulate the compliance properties and respective dynamic behavior of a controlled system. Alongside with the realization of passive compliance within mechanical design [1–4], active compliant control realized within software is increasingly applied in the wider field of robotics including among others industrial settings, such as peg-in-a-hole tasks [5] or human-robot cooperation and co-manipulation [6], medical devices, such as exoskeletons [7] or surgery robots [8], and legged robots [9]. Moreover, compliant control approaches enter industrial practice and, recently, an increasing number of robots is equipped with the required joint force/torque sensors, e.g. Panda (Franka Emika GmbH) [10] and KUKA IIWA (KUKA AG) [11]. These technical systems already have a huge influence on many parts of the society, however, in the future, they will more and more conquer everyday life of individuals in their private as well as in their working environment. That humans and machines get closer in physical interaction - e.g. from collaborative to wearable robots - provides great potential, but also raises the risk of injury in case of unpredicted behavior of human or machine. Hence, safety requirements gain increasing influence, while traditional performance metrics as tracking accuracy remain [12]. Compliance allows to compromise between these conflicting criteria [13, 14]. Passive compliance can improve actuator characteristics such as backdrivability, motor-link decoupling, peak torque and power requirements and energy storage capabilities, but also increases the system complexity and control effort, e.g., to suppress undesired oscillations, and decreases the position or force control bandwidth [14–16]. A solution within software, which is the topic of this review, limits the bandwidth according to the sensor, the actuator and the controller frequency resulting in a rigid behavior for high speed impacts, but keeps the apparent system dynamics more easily adjustable and the mechanical design within certain limits indepen-

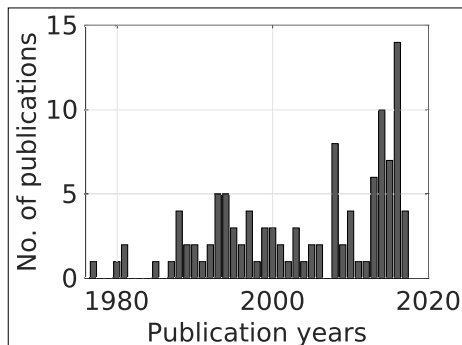


Figure 1: Timeline of publications selected for this review.

dent of the target apparent impedance [15]. Depending on the reflected motor and link inertia as well as the environment’s impedance in contact, already a low passive reflected joint elasticity, such as induced by a Harmonic Drive, can decouple motor and link and hence achieves similarly fast impact characteristics as its more compliant counterpart [14].

The timeline of publications identified and selected during our literature analysis (Fig. 1) underlines the long-lasting and ongoing interest of the research community in the topic of compliant control and hence its maturity but also actuality. The latter gets apparent in the high quantity of recent publications, revealing the importance of a new and enduringly up-to-date review for the scientific discourse. Compliant control has been thoroughly reviewed with respect to the four basic approaches which are *Hybrid Force/Position Control* (HC), *Parallel Force/Position Control* (PC), *Impedance Control* (IC) and *Admittance Control* (AC) [17–32]. Vukobratović [18] provides an extensive introduction into the background and classification of compliant control as well as some variants and combinations of the basic concepts. This is complemented by an overview of the historical development of interaction control presented in Leylavi Shoushtari et al. [31], where also an analysis of the approaches with respect to the criteria stability, generalization, impedance variability, and controllability is given. Further authors focus specifically on insights into the stability properties [17, 26], robustness characteristics [27], and an in-depth study of the characteristics of basic impedance and admittance control for rigid or fixed-compliance systems

[29].

While previous reviews analyzed the basic concepts as well as some variants  
55 and combinations [18, 28, 31], a recent, systematic, and hence transparent and  
comprehensive survey of the emerging field of compliant control does not yet  
exist. With the present review we intend to close this gap. A detailed docu-  
mentation of the literature research yields a clearly stated baseline for further  
60 research or adaption to individual needs, since the results are easily extend-  
able with respect to the content and considered time span in the future. This  
reveals the lasting quality of the paper. An elaborate analysis of the basic con-  
cepts for compliant control results in a multisided and concise summary of their  
characteristics and a classification of a large number of state-of-the-art vari-  
ants of compliant control approaches alongside with their particular objectives.  
65 Although providing some remarks on the treatment of more complex systems,  
the main focus of this review is on individually operating, stiff, non-redundant  
mechanisms. Hereby, a broad and at the same time deep insight into compli-  
ant control is facilitated to the readers. To guide through the complex task  
of selecting the adequate approach from the variety of existing methods and  
70 ease the access to the topic, we subsequently derive and propose a selection  
scheme. Consequently, the presented review enhances and accelerates the above  
described scientific and technological developments.

This review is organized into four sections: Following this introduction, Sec-  
tion 2 introduces general background concepts and the methodology applied to  
75 the literature research in this paper. Section 3 introduces the selection scheme,  
classifies the literature findings and characterizes the basic control concepts for  
modifying the compliance of a system as well as their variations and combina-  
tions. The main findings are discussed in Section 4. Finally, Section 5 concludes  
the paper with a summary of the main contributions and an outlook to future  
80 trends.

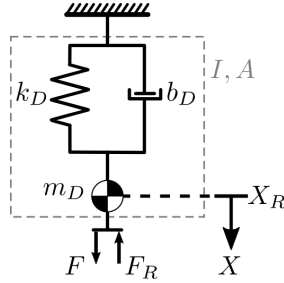


Figure 2: Second order impedance or admittance with the mass  $m_D$ , damping  $b_D$  and stiffness  $k_D$ .

## 2. Background and Methodology

The stiffness, compliance, impedance and admittance characteristics of a mechanism are aimed to be modified by compliant control. Backdrivability as an inherent system property influences the selection and implementation of a particular control approach. In this section, these terms are defined and introduced alongside with the literature research methodology for the further use in this paper.

### 2.1. Stiffness/Impedance and Compliance/Admittance

Stiffness and compliance describe the static relation, while impedance  $I(s)$  and admittance  $A(s)$  refer to the dynamic relation

$$I(s) = \frac{E_F(s)}{E_X(s)} = A^{-1}(s) \quad (1)$$

between the deviation in force  $E_F(s) = F_R(s) - F(s)$  and displacement  $E_X(s) = X_R(s) - X(s)$  with the Laplace variable  $s$ .  $X_R(s)$ ,  $X(s)$ ,  $F_R(s)$  and  $F(s)$  refer to the reference and measured position and force respectively. The order of an impedance or admittance then refers to the highest exponent of  $s$  which reveals stiffness/compliance to be equal to the zeroth order case of impedance/admittance. Figure 2 illustrates the second order case. Alternatively, some authors define impedance and admittance as the force-velocity relation [17, 19] instead of the force-position relation [18, 31, 33]. This complies with Hogan [34], who analogously defined impedance to convert flow input into an

effort output and admittance to accept effort as an input and return flow as an output. If two systems dynamically interact with each other, they must  
100 complement one another, meaning that, if the environment exhibits admittance characteristics, the mechanism should have impedance behavior and vice versa.

## *2.2. Backdrivability*

In case of an ideally backdrivable mechanism, the force that needs to be overcome externally to cause a user-driven displacement [35], tends to zero. In  
105 a non-ideal scenario, backdrivability is limited by acceleration- and velocity-dependent influences and hence the required external force does not reach zero. The acceleration-dependent backdriving, i.e. impeding, force is caused by the moving mass or inertia, whose magnitudes usually raise with the peak torque, the actuation is designed for. Velocity-dependent backdriving forces stem from  
110 friction and damping [36]. The dominance of either of the influences also depends on the mechanical design as well as the application: non-fading, i.e., sudden, loads, such as occurring in case of a collision with a stiff environment, provoke high acceleration-dependent peaks in the backdriving force. Contrarily, in case of fading loads, e.g. resulting from impacts with soft environments, the  
115 acceleration-dependent influence is low relative to the velocity-dependent terms.

High transmission ratios increase the ability to deliver motor force to the environment but decrease or even impede backdrivability as inertia and friction reflected to the output are magnified. Apart from mechanical design considerations, backdrivability can be improved by closed-loop control with a force  
120 sensor at the end-effector of the mechanism [37] or by compensation methods [35, 37–39].

## *2.3. Literature Research Methodology*

For a profound and comprehensive analysis of compliant control approaches, a detailed systematic and free literature research was conducted. The scope of  
125 this review is limited to English language journal articles, conference proceedings, PhD theses, and books.

The systematic research involved seven scientific online databases (ScienceDirect<sup>1</sup>, Web of Science<sup>2</sup>, IEEE Xplore<sup>3</sup>, SAGE journals<sup>4</sup>, WTI Tecfinder<sup>5</sup>, Engineering Village<sup>6</sup>, science.gov<sup>7</sup>). To target comprehensiveness, five search cycles were performed with different thematic fields for search term generation, each of them refined step-by-step until the respective search engine found a maximum of 50 results. The limitation to 50 findings appeared reasonable as it helped to suppress publications of other contexts such as electrical instead of mechanical impedance, but already included cross-references. For an emphasis on recent publications, while still relevance is given to development over time, each search cycle was carried out twice, once limited to publications until 2015 and once restricted to publications of the last three complete years, 2015 to 2017, revealing a total of more than 1,000 results. Based on a first scanning eliminating redundancy and assessing titles, abstracts and keywords, 221 publications were selected. In a second step, further filtering additionally included the full text and especially control relevant sections as well as the novelty of the control approach with respect to the other publications. Finally, a total number of 76 publications was selected for this review.

The complementing free research was realized in three further search engines (Google Scholar<sup>8</sup>, library search engine of TU Darmstadt<sup>9</sup>, Springer Link<sup>10</sup>). Hereby, keywords were not fixed, but key references or authors of previously analyzed publications were traced to get a deeper insight into the topic. This resulted in 33 additional publications to be considered.

Figure 3 summarizes the literature research methodology. A detailed documentation can be found in the Appendix. The results are presented in the

---

<sup>1</sup><https://www.sciencedirect.com/>

<sup>2</sup><http://apps.webofknowledge.com/>

<sup>3</sup><https://ieeexplore.ieee.org/>

<sup>4</sup><http://journals.sagepub.com/>

<sup>5</sup><https://tecfinder.wti-frankfurt.de/>

<sup>6</sup><https://www.engineeringvillage.com/>

<sup>7</sup><https://www.science.gov/>

<sup>8</sup><https://scholar.google.com/>

<sup>9</sup><https://www.ulb.tu-darmstadt.de/>

<sup>10</sup><https://link.springer.com/>

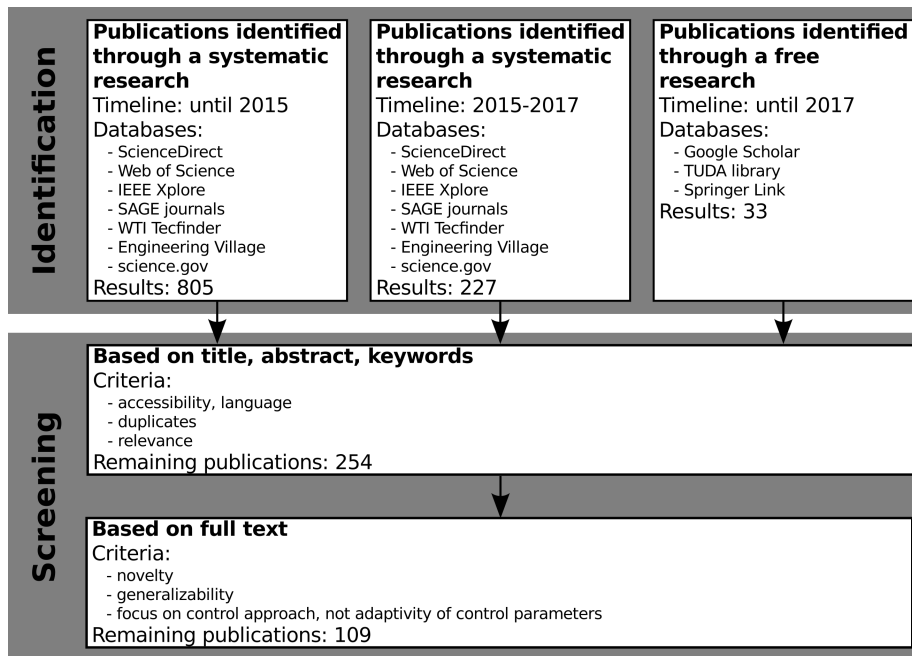


Figure 3: Applied literature research methodology.

following section.

### 3. Control Concepts

Compliance can be achieved and manipulated by changing the inherent characteristics of a mechanism (passive compliance) or by control (active compliance). With the term *active compliant control* not being consistently specified in literature [18, 29, 40], for this work, it is defined as the simultaneous and purposeful control of deviations in position and force. Similar to [18], the four fundamental compliant control approaches, hybrid and parallel force/position control, impedance and admittance control, can be organized as depicted by Table 1.

In direct force control, the force feedback loop is closed by a force controller. By contrast, in indirect force control, force control is realized through motion control. This inner or outer motion control loop enables the establishment of a desired relation between system motion and force [26, 33, 41].



Table 1: Classification of fundamental approaches of compliant control

	Explicit control	Implicit control
Direct control	<ul style="list-style-type: none"> <li>• Hybrid Force/Position Control</li> <li>• Parallel Force/Position Control</li> </ul>	-
Indirect control	<ul style="list-style-type: none"> <li>• Impedance Control</li> <li>• Admittance Control</li> </ul>	<ul style="list-style-type: none"> <li>• Impedance Control</li> </ul>

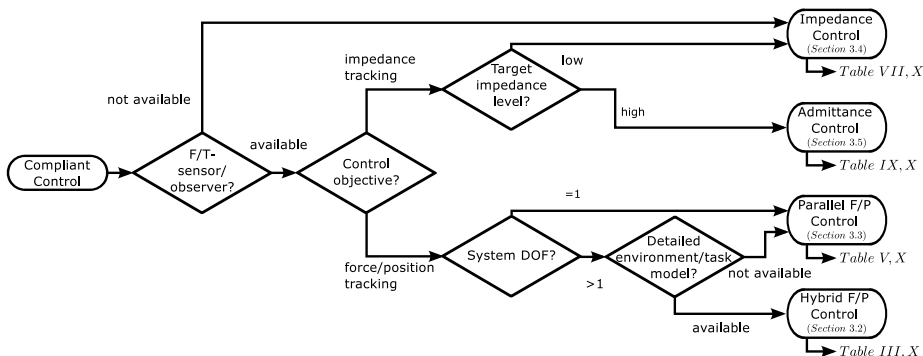


Figure 4: Selection scheme for compliant control approaches.

165 Explicit force control is characterized by force feedback with the use of a force sensor, while in the implicit case the actuator input is provided by open loop control and through the difference between the target and measured motion [33, 42]. Implicit force control is only applicable for backdrivable systems [37] with negligible friction influence and, due to its impact reaction characteristics, 170 only advisable for slow velocities and soft environment surfaces [42]. To alleviate these limitations by predicting the missing force sensory information, a system and environment model is required.

In this review, it is assumed that lower level controllers linearize and decouple the system dynamics while a higher level controller shapes the required 175 compliant system behavior.

### 3.1. Selection Scheme

Apart from the four main concepts of compliant control, numerous specialized variants and combinations of approaches can be found in literature. For an easy orientation and support for the selection of an appropriate approach, we 180 propose the scheme illustrated by Figure 4.

Most compliant control approaches require force/torque (F/T) data to be available, which can be provided by sensors or observers. Otherwise, the implementation is limited to implicit impedance control, which is also indicated by Table 1. The control objective is a design decision. While hybrid and parallel  
185 force/position control aim at tracking a target force or position, impedance and admittance control regulate their relation, but not explicitly their individual trajectories. The level of this relation or impedance is an indicator whether impedance or admittance control is more beneficial for the stability characteristics of the closed-loop system. The hybrid force/position control approach  
190 requires the system to have multiple degrees of freedom (DOF) and a detailed environment and task model to enable the division of the working space in position- and force-controlled subspaces according to the environmental constraints. If these conditions are fulfilled, it can be beneficial to be applied as it allows to exploit the model knowledge and it provides faster dynamics and  
195 reduced design complexity compared to the more robust parallel force/position control approach.

All in all, the scheme is an attempt to summarize the main restrictions for the implementation of compliant control approaches and guide an appropriate selection from the main control concepts. After identifying one of them as  
200 suitable, Sections 3.2 to 3.5 provide a deeper analysis of their characteristics and variants. Especially the latter and in particular their individual objectives can be employed for fine tuning. If the characteristics of more than one main approach are required, a compound control approach, as reviewed in Section 3.6 might be an adequate fit.

### 205 3.2. Hybrid Force/Position Control (HC)

The force-based or explicit hybrid force/position control approach goes back to Mason's concept published in 1981 [46] and was firstly proposed in its present form by Raibert and Craig [44]. The compliance selection matrix  $S = \text{diag}(s_j)$ , with  $j = 1 \dots n$  and  $n$  being the number of degrees of freedom, divides the workspace into complementary orthogonal subspaces, which are either motion-

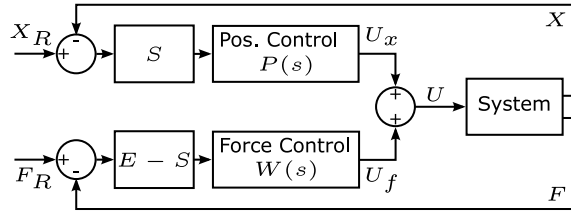


Figure 5: Hybrid force/position control scheme [17, 23].

Table 2: Strengths and weaknesses of hybrid force/position control [17, 18, 20, 22, 23, 25, 31, 41, 43–45]

<ul style="list-style-type: none"> <li>⊕ Possibly mature</li> <li>⊕ Independent design and implementation of position and force control law</li> <li>⊕ Force and position trajectory tracking within respective subspaces</li> <li>⊕ Low complexity for planar surfaces</li> <li>⊕ Effective for high stiffness environments</li> </ul>	<ul style="list-style-type: none"> <li>⊖ No standard feature of industrial robots</li> <li>⊖ Orthogonal subspaces</li> <li>⊖ Stability issues due to discreteness</li> <li>⊖ No specific manipulator impedance</li> <li>⊖ Complexity for non-planar surfaces</li> <li>⊖ Requires detailed environment model</li> <li>⊖ Force measurement required</li> <li>⊖ Not robust to (unpredicted) task changes</li> <li>⊖ Performance depends on system configuration</li> </ul>
---	---

or force-controlled. While motion-constrained directions must be force-controlled ( $s_j = 0$ ), free directions need to be motion-controlled ( $s_j = 1$ ). The subspaces and their corresponding constraint types are derived from a detailed environment model, which is always required for hybrid force/position control [41]. Furthermore, the implementation on standard industrial robots is generally limited as the latter are mostly only position-, but not force-low-level-controlled and hence do not support the hybrid structure [22]. The knowledge of system dynamics is not mandatory [47]. In Khalil et al. [23] and An et al. [47], possible

stability issues are discussed. Figure 5 illustrates the control concept given by

$$U(s) = S \cdot P(s) \cdot (X_R(s) - X(s)) + (E - S) \cdot W(s) \cdot (F_R(s) - F(s)). \quad (2)$$

Hereby,  $U(s)$  represents the control output with the indices  $x$  for position and  $f$  for force.  $P(s)$  and  $W(s)$  are the position and force control law and their structure and parameters can be selected according to the system characteristics and implementation objectives. In literature, they are often selected following a  
 210 PID approach [17, 18]. The respective lower case characters refer to the upper case variable in time domain.  $E$  is the identity matrix of size  $n \times n$ . The system block can include an inner control loop as in Yoshida et al. [48].

Table 2 summarizes the Strengths and weaknesses of the basic hybrid force/  
 position control approach. Hereby, maturity is justified by the stagnation w.r.t.  
 215 recent publications, which would highlight new issues [22], however, it might also be argued, that the research interest has rather been shifted to other basic approaches. Variants and advanced configurations of hybrid force/position control are introduced in Table 3 and address the solution of some of these drawbacks, such as the implementability for standard position-controlled industrial  
 220 robots, the requirement of an environment model, and the limitation to orthogonal subspaces. The robustness to unpredicted task changes remains an open challenge [31], to which the parallel force/position control approach described in the next section is directed.

Table 3: Variants of hybrid force/position control.

Approach	Objective	Ref.
<b>Position-based or Implicit HC:</b>		
At the price of reduced force tracking performance, the environment model is used within the force control in order to map the force error to an equivalent position which is then added to the reference input of the unchanged inner loop position control.	→ reliability (standard inner position control loop) → robustness to parameter/task variation	[23, 25]

Table 3 (Continued): Variants of hybrid force/position control.

Approach	Objective	Ref.
<p><b>Implicit/Explicit Force Control:</b> The approach combines force- and position-based HC by merging their force control laws.</p>	→ combines strengths of both individual concepts	[25]
<p><b>Adaptive HC:</b> The division in subspaces is realized through the reference trajectory which serves as input for a position controller. The desired force is scaled depending on the environment stiffness.</p>	→ interaction with unknown stiffness environment	[49]
<p><b>Resolved Acceleration Based Approach:</b> System dynamics are included into the control law.</p>	→ compensation for system dynamics	[23, 25, 26]
<p><b>Not-Orthogonal Hybrid Control:</b> Extension of dynamic hybrid control, that transforms the mechanism and environment models into two independent equations, creating two not necessarily orthogonal subspaces.</p>	→ no need for orthogonal subspaces	[43]

### 3.3. Parallel Force/Position Control (PC)

Parallel force/position control has been firstly proposed by Chiaverini and Sciavicco in 1988 [51]. As well as for hybrid force/position control, the objective consists in tracking the reference motion trajectory in unconstrained directions and in controlling the contact forces arising in constrained directions. Unlike

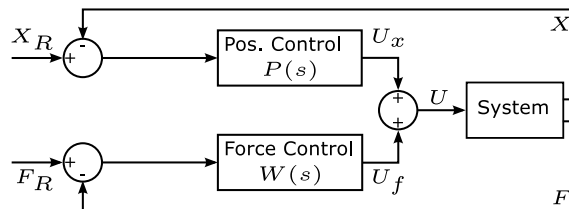


Figure 6: Parallel force/position control scheme [45].

Table 4: Strengths and weaknesses of parallel force/position control [21, 41, 45, 50]

⊕ Force and position trajectory tracking	● No standard feature of industrial robots
⊕ Robustness and safety in the presence of environment model uncertainties and planning errors	● No specific manipulator impedance
⊕ Robustness to (unpredicted) task changes	● Force measurement required
	● Slower dynamics and increased complexity compared to hybrid approach

in hybrid force/position control, in parallel force/position control the force and motion controller outputs are superimposed and can hence act on the same directions. In literature, the combination of a PD position and a PI force control approach is proposed [18, 21]. The dominant integrator as part of the force control law causes the steady-state force error to be driven to zero at the expense of a motion error [21]. The influence of position and force control can be weighted by their feedback gains [22] and the control law can be extended by a system dynamics compensation term [20, 45]. The system stability and an inner position control loop for friction compensation are discussed in Flixeder et al. [30]. Figure 6 shows the general control concept given by

$$U(s) = P(s) \cdot (X_R(s) - X(s)) + W(s) \cdot (F_R(s) - F(s)). \quad (3)$$

225 Table 4 summarizes strengths and weaknesses of parallel force/position control and its extensions and variants are introduced in Table 5. The first five approaches discuss and modify the influence of the system model on the control performance. Further approaches aim at decoupling the position and force control loop, an improved force tracking and an adaption of the parallel concept  
 230 to cooperative multi-manipulator control. Compared to the hybrid approach, parallel force/position control does not require knowledge about the task and environment. A thorough analysis and comparison are provided by Chiaverini et al. [45].

Table 5: Variants of parallel force/position control.

Approach	Objective	Ref.
<b>Parallel Force/Position Regulation:</b> Static instead of dynamic model-based compensation is applied.	→ simplified system model at the cost of tracking performance	[21, 41]
<b>Adaptive Force/Position Regulation:</b> An adaptation law for gravity compensation within parallel force/position regulation is presented.	→ loosens the requirement for exact gravity force model parameters	[41]
<b>Passivity-Based Control:</b> The dynamic model-based compensation parameters are adapted online.	→ robustness to model parameter errors	[41, 50, 52]
<b>Robust Adaptive Force/Position Control:</b> A model-based parallel force/position control approach is extended by an error compensation term.	→ robustness to model errors, joint friction, environment disturbances	[53]
<b>Output Feedback Control:</b> A (non)linear observer replaces the need for velocity feedback within force/position regulation and passivity-based control respectively.	→ no velocity measurement required	[41]
<b>Force/Position Control with Full Parallel Composition:</b> The force controller contains a double integration of the force error.	→ force error dynamics independent of position error dynamics	[41]
<b>Contact Stiffness Adaptation:</b> Contact stiffness estimation and the derivatives of a time-varying desired force are included into the control law which is based on full parallel composition.	→ improved (transient) force tracking behaviour at the cost of a larger position error	[41]
<b>Multi-Manipulator Parallel Force/Position Control:</b> The target trajectory is commanded in the cooperative task space and then transformed into the respective manipulator task spaces.	→ cooperative multi-manipulator control	[54, 55]

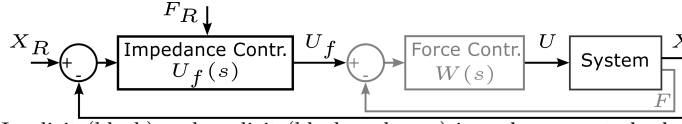


Figure 7: Implicit (black) and explicit (black and grey) impedance control scheme [33, 56].

Table 6: Strengths and weaknesses of impedance control [21, 31, 33, 34, 57–61]

⊕ Implements motion/force relation	⊖ No standard feature of industrial robots
⊕ Robustness to task uncertainty (e.g. environment) and changes	⊖ No exact tracking of position and force
⊕ Physically meaningful parameters ( $m \leq 2$ )	⊖ Sensitive to system modelling errors
⊕ Accuracy (compared to AC)	⊖ Accuracy/Z-width dilemma
⊕ Superposition property	⊖ Stability issues for high target impedances and due to force control (explicit)
⊕ No force measurement required (implicit)	⊖ Backdrivability necessary (implicit)

### 3.4. Impedance Control (IC)

Impedance control is synonymously called force-based impedance control, impedance control without force feedback or equilibrium point control. It goes back to Hogan’s proposal of 1985 [34] and focuses on the implementation of a target relation between force and motion, but does not necessarily track their individual trajectories [21]. Therefore,  $X_R(s)$  is also called rest instead of reference position. The position  $X(s)$  is measured and conclusions for the inner loop reference force  $U_f(s)$  are drawn by means of the mechanical impedance  $I(s)$  which is reflected by the linear impedance control law as polynomial of  $m^{\text{th}}$  order with the parameters  $a_k$ :

$$U_f(s) = I(s)(X(s) - X_R(s)) + F_R(s), \quad \text{with } I(s) = \sum_{k=0}^m a_k \cdot s^k. \quad (4)$$

235 As illustrated by Figure 7, impedance control can be implemented explicitly or implicitly [33, 37], where in the first case, a compromise for a well performing but stable force controller is to be found [33].



Choosing the impedance parameters means deciding for a tradeoff between the allowed contact force and deviation from the reference motion trajectory.

240 For a targeted high system to environment stiffness ratio, the system endpoint tends to reach the desired steady-state rest position at the expense of penetration into the environment. For a low ratio, the endpoint rather adopts to environmental constraints [62]. A method for impedance controller synthesis by optimization is introduced in Hogan (1985) [34]. An analysis of the stability and passivity of impedance control and a deduction of a procedure for the controller design are provided in Ott [56] and Boaventura et al. [61]. Yoshikawa [20] mentions a progressive learning method. General recommendations for the impedance controller synthesis can be found in Khalil et al. [23]. The achievable range of the end-effector target impedance and its corresponding feasibility region with respect to  $X_R$  are limited by the design of the mechanism, which influences its configuration and actuator boundaries [63] as well as the occurrence of singularities [56].

245

Impedance control is suitable for small desired impedance levels. Contrarily, the resulting high control gains possibly cause stability issues or conflict with accuracy requirements. Countermeasures are increased friction (implicit) or actuator bandwidth (explicit) [33]. As in constrained space, an end-effector impedance always counteracts an environmental admittance, which converts the incoming sum of forces to a change in motion, multiple parallel impedances even related to different  $X_R$  can be superimposed. In free space, impedance control behaves like a motion controller [64]. While in certain cases a model-free implementation might be sufficient [34], target impedance tracking can be improved by a dynamic system model as introduced for example in Yoshikawa [20], Siciliano et al. [41], and Valency et al. [60]. The characteristics of the controller implementation in joint or Cartesian space are discussed in Khalil et al. [23]. In Sharifi et al. [8], a master-slave approach is proposed. In the case of contact with a stiff environment, impedance control can be related to explicit force control [65]. In Table 6 the strengths and weaknesses of impedance control are summarized.

250

255

260

265

In the following, the special cases  $m \in \{0, 1, 2\}$  are considered in more detail. While the general approach theoretically allows for  $m > 2$ , the reviewed publications do not mention the practical implementation of such higher order impedance controllers. Subsequently, variants of impedance control found in literature are introduced in Table 7. They aim at improvements concerning implementation issues, target position, force and impedance tracking or the intelligent management of system redundancies, loosening system model or F/T measurement requirements, reduced F/T peaks at contact, the generalization of the (linear) impedance concept or its extension to the multi-robot and object handling case. While most previous considerations were related to the control of the end-effector impedance, object handling requires the consideration of not only the external forces which affect the object dynamics, but also of the internal forces, which affect the object's internal stresses [66–68]. This is related to the control of the external impedance between the object and environment and the internal impedance between the end-effector(s) and object [69]. Compared to the other main concepts, the quantity of variants and their objectives is significantly higher, indicating a certain maturity. Nevertheless, the ongoing research interest is revealed by the distributions of publication dates.

$$\mathbf{m} = \mathbf{0} \Leftrightarrow \mathbf{I}(s) = \mathbf{a}_0 = \mathbf{k}_D:$$

Impedance control of zeroth order or stiffness control [20, 70] has first been mentioned by Salisbury in 1980 [71] and, in its implicit case, is formally equal to a P position controller.  $k_D$  then represents the target stiffness which for free motion should be set to a high and for contact cases to a low value [23].

Generally, for (implicit) stiffness control without or with static model-based compensation [21, 23, 41], force measurement is not required [21]. However, it can be useful for  $k_D$  adjustment [21]. Explicit stiffness control shows increased force sensitivity [71]. Moreover, for an emphasis on force control, a feedforward force term can be added [23, 47, 71].

Stiffness control is less computationally demanding, complex and sensitive to model uncertainties than high-order and dynamic model-based impedance

300 control [23, 60], but also possibly reduces stability and accuracy in the explicit case [20]. Implicit stiffness control is passive [72].

$$\mathbf{m} = \mathbf{1} \Leftrightarrow \mathbf{I}(s) = \mathbf{a}_0 + \mathbf{a}_1 s = \mathbf{k}_D + \mathbf{b}_D s:$$

In damping control, the velocity error ( $\dot{X}_R(s) - \dot{X}(s)$ ) is fed back multiplied  
 305 by the target damping coefficient  $b_D$  [37]. However, pure damping control can barely be found in the literature. Generally, a stiffness term is added which then results in impedance control of the first order [23, 62, 70]. In the implicit case, first order impedance control is formally equal to a PD position controller, possibly extended by a static model-based compensation [73]. Damping has a  
 310 significant influence on stability. The damping coefficient  $b_D$  compensates for natural and induces active damping [70].

$$\mathbf{m} = \mathbf{2} \Leftrightarrow \mathbf{I}(s) = \mathbf{a}_0 + \mathbf{a}_1 s + \mathbf{a}_2 s^2 = \mathbf{k}_D + \mathbf{b}_D s + \theta_D s^2:$$

Generally, the target impedance can be selected to be of arbitrary order, how-  
 315 ever, already Hogan [34] stressed the advantages of the second order as thereby, the inertial dynamics of the system can be manipulated aiming at the target inertia  $\theta_D$ , while the parameters  $a_k$  remain physically meaningful. Implicit second order impedance control is formally equal to PID velocity control. The discrete formulation is given in Xu [74].

Table 7: Variants of impedance control.

Approach	Objective	Ref.
<b>Computed Torque IC:</b> Model-based approach which uses force sensor information to compute the control output.	→ acceleration not required	[62, 75]
<b>Steady State Approximation:</b> Velocities in the dynamic model-based compensation are assumed zero, the inertia constant at the price of reduced accuracy.	→ no inverse Jacobian required → computational effort reduced	[75]

Table 7 (continued): Variants of impedance control.

Approach	Objective	Ref.
<p><b>Task-Space Control With Null-Space Compliance:</b> The redundant DOF of a task-space position controlled robot are used to achieve computed torque impedance control in joint space. Observers to replace F/T-measurement are proposed.</p>	<p>→ position control in task-space, IC in joint space → no F/T-measurement required</p>	[76]
<p><b>Model-Based Generalized IC:</b> The generalized target imp. is defined by <math>(\theta_D s^2 + b_D s + k_D) \cdot (X - X_R) = k_f (F - F_R)</math>, where <math>k_f</math> corresponds to the so-called force stiffness and an extension by an environment model is optional. In case of positive <math>\theta_D, b_D, k_D, k_f</math>, the controlled system is stable.</p>	<p>→ considers reference force trajectory → additional DOF <math>k_f</math> for controller tuning → environment model instead of F/T-measurement</p>	[77, 78]
<p><b>Inertia Shaping Avoiding IC:</b> In task space second order IC with dynamics compensation, the target inertia <math>\theta_D</math> is set equal to the system inertia. Centrifugal and Coriolis terms are considered within the target damping <math>b_D</math>.</p>	<p>→ no F/T-measurement required</p>	[56]
<p><b>Virtual Model Control:</b> The reference force trajectory is generated by a simulation of virtual components inspired by physical counterparts. Inverse dynamics are not used.</p>	<p>→ generalization of the target impedance</p>	[79]
<p><b>Model-Feedforward Open-Loop IC:</b> The time-dependent target parameters for an implicit IC are deduced from the collision simulation of virtual objects.</p>	<p>→ generalization of the target impedance</p>	[80]
<p><b>Indirect Stiffness Control:</b> The virtual spring model for stiffness control is replaced by a potential energy approach.</p>	<p>→ overcomes its limitation to linear virtual springs</p>	[81]
<p><b>Intelligent Control:</b> The angle of attack of the actuator force is adjusted according to the deviation from the reference position trajectory.</p>	<p>→ results in nonlinear stiffness control</p>	[82]

Table 7 (continued): Variants of impedance control.

Approach	Objective	Ref.
<p><b>Force Field Control:</b> The commanded motor torque is divided into a component normal and tangential to the target position trajectory. Both are exponentially related to the position trajectory error.</p>	<p>→ nonlinear stiffness control → position tracking in time and space → safety: position tracking without high torque peaks</p>	[83]
<p><b>Tanh-D IC:</b> The computed torque IC is extended by additional terms accounting for deviations between the target and measured impedance.</p>	<p>→ target impedance tracking</p>	[64]
<p><b>Tanh-Tanh-Type Control:</b> Simulates the behaviour of a nonlinear virtual spring with a saturated dissipative term.</p>	<p>→ reduced deviation between actual and rest position</p>	[81]
<p><b>Reciprocal-Quadratic-Type Control:</b> Simulates the behaviour of a nonlinear virtual spring with a dissipative term, with the control output being inversely proportional to the position deviation.</p>	<p>→ drives the deviation between actual and rest position to zero</p>	[81]
<p><b>Force Tracking IC:</b> Assuming the knowledge of the external force and environment position, the reference position for the IC is modified.</p>	<p>→ focus on force tracking</p>	[84]
<p><b>Force Overshoot-free IC:</b> The rest position (and target impedance parameters) are modified online based on environment and base impedance estimations.</p>	<p>→ focus on force tracking → avoid force overshoot</p>	[85–88]
<p><b>Acceleration-Based Force-IC:</b> An inner acceleration tracking controller is encased by a middle IC loop and an outer nonlinear force control loop.</p>	<p>→ limited contact force → robustness to environment uncertainty</p>	[58]

Table 7 (continued): Variants of impedance control.

Approach	Objective	Ref.
<b>Sliding Mode IC:</b> Variant of (generalized) IC implemented by sliding mode control, possibly extended by disturbance estimation.	→ robustness to model uncertainties, disturbances → stable despite of nonlinear system dynamics	[74, 77, 78, 89]
<b>Robust Compliant Control Using Time Delay Estimation:</b> Time delay estimation with ideal velocity feedback (C1) or modified target damping (C2) or internal model control (C3) suppresses the effects of (dis-) continuous uncertainties in the system dynamics.	→ no system model required (C1-C3) → target impedance tracking (C1, C3) → position tracking (C2)	[90–93]
<b>Pose Improved Stiffness Control:</b> Extension of stiffness control which exploits the redundancy of the manipulator for null-space pose adjustment.	→ optimal stiffness feasibility region → minimal gravity effect → avoid torque saturation	[63]
<b>Object IC:</b> This version of computed torque IC implements the target impedance related to the manipulated object instead of the mechanism’s endpoint.	→ multi-robot object handling → object dyn. compensation → weightable load/DOF distribution	[66, 67]
<b>Multiple IC:</b> This extended version of object IC establishes a target impedance at the cooperating mechanisms’ endpoints and at the commonly manipulated object’s level.	→ multi-robot object handling → improved stability → smooth dynamic behaviour	[66]
<b>Internal Force-Based IC:</b> Within the computed torque IC approach, the total measured force is replaced by the non-motion-inducing internal force.	→ multi-robot object handling → object dynamics not required	[68]

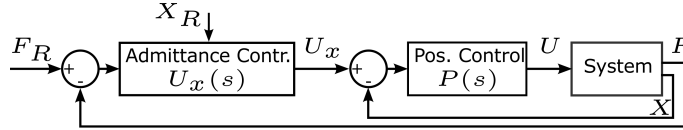


Figure 8: (Explicit) admittance control scheme [56].

Table 8: Strengths and weaknesses of admittance control [21, 33, 41, 59, 60, 69, 94, 95]

⊕ Implements motion/force relation	⊖ No exact tracking of position and force
⊕ Robustness to task uncertainty and changes	⊖ Force measurement required
⊕ System/environment model not required	⊖ Impedance tracking accuracy (compared to impedance control)
⊕ Backdrivability not required	⊖ Stability issues for low target impedances
⊕ Inner position loop: standard feature of industrial robots, free space position tracking, disturbance rejection	
⊕ Physically meaningful parameters ( $m \leq 2$ )	
⊕ Acceleration not required	

### 320 3.5. Admittance Control (AC)

Admittance control (AC) which is also called position-based impedance control or impedance control with force feedback is an approach dual to impedance control. As presented by

$$U_x(s) = A(s)(F(s) - F_R(s)) + X_R(s), \quad \text{with } A(s) = \left( \sum_{k=0}^m a_k \cdot s^k \right)^{-1} \quad (5)$$

for the linear case, the mechanical admittance  $A(s)$  relates the measured external force  $F(s)$  to the reference motion  $U_x(s)$  for the inner position control loop. The computation of the reference motion in time domain requires numerical integration.

325 Admittance control can be implemented explicitly as shown in Figure 8 or implicitly. For implicit admittance control, the outer force feedback loop is excluded. Therefore, depending on the selection of the inner loop position control law, implicit admittance control is equivalent to implicit impedance

control. Hence, implicit admittance control is commonly not considered [33].

330 Impedance and admittance control distinctly differ in their capabilities to render certain target impedance levels and in the key characteristics of their inner control loop. While for IC a high target impedance level results in high control gains, which possibly cause instability, AC is prone to instability in case of a low target impedance level. For both, IC and AC, a high target impedance  
335 level can cause stability issues during contact with a stiff environment. As methods for setting the admittance parameters, the linear quadratic control approach [96] and a learning approach based on the betterment scheme [97] are proposed. Moreover, for impedance control, a compromise between good disturbance rejection and target position tracking accuracy, which require a  
340 high stiffness gain  $k_D$ , and compliant behavior, which needs a low stiffness gain, has to be found. Admittance control overcomes this conflict due to the inner motion control loop [98], which is a standard feature of industrial robots and has the potential to suppress unwanted influences of the system dynamics such as friction without the requirement of a model. Table 8 summarizes further  
345 strengths and weaknesses of admittance control.

The control structure of the inner motion control loop can be selected arbitrarily, but stable [60]. It is further necessary to compute the inner loop with a significantly higher bandwidth than the outer loop [99]. In literature, a broad variety of approaches, ranging from PID control [9, 60, 94, 95, 100, 101] to  
350 more sophisticated concepts [97–99, 102], are proposed for combination with admittance control.

Subsequently, the special cases of admittance control with  $m \in \{0, 1, 2\}$  are considered in more detail. While the general approach theoretically allows for  $m > 2$ , the reviewed publications do not mention the practical implementation  
355 of such higher order admittance controllers. This is followed by an introduction of the variants of admittance control found in literature in Table 9. They aim at loosening the F/T measurement requirement, an improved target position, force or admittance tracking performance including a suggestion for a compromise for the accuracy/robustness dilemma, solving the stability issue of high



360 target admittances, a generalization of the admittance concept or the extension  
to a cooperative control of multiple robots. It is worth to remark that all draw-  
backs listed in Table 8 are addressed by at least one of the variants. Hence,  
the admittance control approach might be a good option for a compromising,  
general purpose control.

365

$$\mathbf{m} = \mathbf{0} \Leftrightarrow \mathbf{A}(s) = \mathbf{a}_0^{-1} = \mathbf{k}_D^{-1}:$$

Admittance control of zeroth order or compliance control [42] is the counterpart  
to stiffness control. The control parameter selection can be related to the sys-  
tem stability [103, 104]. Stiffness and compliance control can also be referred  
370 to by a generalized spring as in [46] or by artificial or active compliance [37].

$$\mathbf{m} = \mathbf{1} \Leftrightarrow \mathbf{A}(s) = (\mathbf{a}_0 + \mathbf{a}_1 s)^{-1} = (\mathbf{k}_D + \mathbf{b}_D s)^{-1}:$$

Admittance control of first order or accommodation control [42, 59] has already  
been mentioned by Whitney in 1977 [105]. It is an approach dual to damping  
375 control and synonymously named active accommodation or generalized damping  
[37, 46]. Accommodation control is especially relevant for slow motion applica-  
tions as the inertia characteristics of the closed-loop system are negligible in this  
case [100]. The system stability has been analyzed by Whitney [104, 105] and  
Ugurlu et al. [9]. A discretized form can be found in Zhou et al. [106]. In Tang  
380 et al. [5], it is proposed to learn the state-dependent admittance parameters by  
Gaussian Mixture Regression.

$$\mathbf{m} = \mathbf{2} \Leftrightarrow \mathbf{A}(s) = (\mathbf{a}_0 + \mathbf{a}_1 s + \mathbf{a}_2 s^2) = (\mathbf{k}_D + \mathbf{b}_D s + \mathbf{m}_D s^2)^{-1}:$$

Admittance control of second order allows to manipulate the inertia character-  
385 istics of the system. Nevertheless, unlike for impedance control (without force  
measurement), the computation of the possibly noisy second order derivative of  
the position measurement can be avoided. In Volpe et al. [94], (second order)  
admittance control is related to direct force control and their conversion is de-  
rived. An instability index can be used to adjust the admittance parameters  
390 according to the environment characteristics [6]. Alternatively, conditions which  
need to be met by the admittance parameters can be derived from passivity cri-

teria [9].

Table 9: Variants of admittance control.

Approach	Objective	Ref.
<p><b>AC without Force Sensor:</b> The external force is estimated based on a generalized momentum based observer.</p>	→ no force measurement required	[95]
<p><b>Frequency-Shaped IC:</b> A disturbance observer modifies the apparent target compliance depending on the frequency of the external force.</p>	→ safety, position tracking, robustness to perturbation → no F/T-measurement required	[107]
<p><b>Instantaneous Model IC:</b> The target impedance is solved for <math>\ddot{x}_R</math>, integrated and fed into the inner loop position control. Thereby, the integration is re-initialized to the current state of the manipulator at each time step.</p>	→ tradeoff between robustness to modelling errors (AC) and target impedance tracking accuracy (IC)	[60]
<p><b>Force/IC with Feedback Linearization:</b> The AC is extended by an exact linearization control loop. The latter computes the reference force for the AC which is required to achieve a desired force. An environment model is needed.</p>	→ force tracking	[108]
<p><b>Iteratively Learned and Temporally Scaled Force Control:</b> Iterative learning control is applied to modify the target position trajectory for a first order AC.</p>	→ increased execution speed while maintaining target force trajectory	[109]
<p><b>Natural AC (NAC):</b> The outer first order AC loop undergoes a model-based modification. The inner velocity control loop consists of a target impedance and a proportional admittance tracking error compensation term.</p>	→ passivity including for high admittances	[110, 111]

Table 9 (continued): Variants of admittance control.

Approach	Objective	Ref.
<b>Neuromechanical Control:</b> The virtual model is composed of an antagonistic pair of muscles, represented each by a first order admittance with a parallel contractile element (Voigt's muscle model), connected to an inertial joint. The contractile elements are regulated by a neural network and serve as exciting element.	→ biological analogy	[112]
<b>Admittance Feed Control:</b> The zeroth order admittance is multiplied by a newly introduced time-varying matrix to provide a framework for constrained AC.	→ anisotropic constrained AC	[113, 114]
<b>Cooperative AC:</b> Approaches similar to the internal force-based IC and the object IC are combined to achieve internal and external impedance control.	→ multi-robot object handling → geometrically consistent stiffness	[69]

### 3.6. Compound Control

Combinations of the four basic approaches and their variants, as presented in  
 395 Table 10, generally aim at unifying their strengths, if not indicated otherwise.  
 The first five concepts replace a position or force control loop within hybrid  
 or parallel force/position control by impedance or admittance control, thereby  
 modifying the control objective of this direction. Unified impedance and admit-  
 tance control is especially interesting to improve stability and performance in  
 400 the presence of an environment with diverse impedance properties. Nested com-  
 pliant admittance control focuses on the reduction of geometric misalignment  
 and interaction forces during peg-in-hole tasks. The last approach addresses  
 compliant control of wheeled manipulators.

Table 10: Compound control concepts.

Approach	Basic Concepts	Ref.
<p><b>Hybrid IC:</b> Position- or force-controlled subspaces can be replaced by impedance- or admittance-controlled subspaces, thereby assigning individual target impedances to them.</p>	<ul style="list-style-type: none"> <li>• HC</li> <li>• IC and/or AC</li> </ul>	[17, 22, 27, 115, 116]
<p><b>Unified IC and HC with Kinesthetic Filtering:</b> Within HC, position control is replaced by IC. The selection matrix is realized through kinesthetic filtering for invariance to reference frame transformations.</p>	<ul style="list-style-type: none"> <li>• HC</li> <li>• IC</li> </ul>	[117]
<p><b>Force/IC:</b> Certain subspaces of HC can be selected to behave compliantly while their orthogonal counterparts are characterized by force control.</p>	<ul style="list-style-type: none"> <li>• HC</li> <li>• computed torque IC</li> </ul>	[101]
<p><b>Hybrid NAC/Position Control:</b> Certain subspaces of HC can be selected to behave compliantly while their orthogonal counterparts are characterized by position control.</p>	<ul style="list-style-type: none"> <li>• HC</li> <li>• NAC</li> </ul>	[111]
<p><b>Parallel Admittance/Position Control:</b> Within the PC framework, the force controller is replaced by AC.</p>	<ul style="list-style-type: none"> <li>• PC</li> <li>• AC</li> </ul>	[118]
<p><b>Unified IC and AC:</b> Realizes time-based interpolation between IC and AC.</p>	<ul style="list-style-type: none"> <li>• IC</li> <li>• AC</li> </ul>	[119]
<p><b>Nested Compliant AC:</b> An IC is encased by an AC to estimate the environment position and thereby reduce contact forces and compensate for position misalignment.</p>	<ul style="list-style-type: none"> <li>• IC</li> <li>• AC</li> </ul>	[120]

Table 10 (continued): Variants of admittance control.

Approach	Basic Concepts	Ref.
<b>Whole-Body IC for Wheeled Manipulators:</b> Impedance and admittance controlled subsystems are interconnected with the aim of compliantly whole-body controlling mobile, including nonholonomic, systems.	<ul style="list-style-type: none"> <li>• IC</li> <li>• AC</li> </ul>	[121]

### 3.7. Further Concepts

405 Compliant control develops its full potential when the task involves contact scenarios. In Yoshikawa [20] and Volpe et al. [122], special consideration of the transition phase between free and constrained motion is proposed for stable contact. Suggestions include maximal active damping, integral explicit force control, proportional force control with reaction force compensation or  
 410 with negative gain and feedforward signal or second order impedance control with a large target mass. These considerations might find their way into the improvement of the contact stability of the main concepts.

The approaches related to the four main compliant control concepts reviewed above are prominent in literature; however, it is worth to mention that compliance  
 415 can also be achieved by learning strategies such as Fuzzy Reinforcement Compliance Control [123] or Dynamic Movement Primitives [124]. A detailed review of learning strategies for compliant control is outside the scope of this paper.

## 4. Discussion

420 The chronological order of the above presented findings as well as a comparison with the previous review of Vukobratović [18] indicate a shift of the research interest from the earlier approaches HC and PC to the more recent impedance and admittance control concepts since the beginning of this millennium. This

425 shift is less pronounced for the compound approaches, where HC or PC are combined with IC or AC to unify their strengths. Compared to the other fundamental compliant control concepts, an outstanding amount of variants of IC reflects its continued popularity during the last decades.

Table 11: Comparison of the main distinguishing features of the basic control concepts and the potential of their variants to improve them (c. stands for control, env. for environment, dom. for dominant, opt. for optimal, and backdriv. for backdrivability).

	HC	PC	IC	AC
C. target	$\varphi, \tau$	$\varphi, \tau$ (dom.)	$I(s)$	$I(s)$
System model	to improve c. performance	to improve c. performance	to improve c. performance	not required
Env. model	required	not required	not required	not required
Task change robustness	no	yes	yes	yes
F/T data required	yes	yes	impl. IC: no expl. IC: yes	yes
Low-level c.	$\varphi, \tau$	$\varphi, \tau$	$\tau$	$\varphi$
Advantageous contact type	stiff	not specified	stiff	soft
Backdriv. required	no	no	impl. IC: yes expl. IC: no	no
Main potential of variants	low-level $\tau$ -c. not required, task change robustness, unknown stiffness interaction, non-orthog. subspaces	robustness to sys. model uncertainty, independent $\varphi$ -/ $\tau$ -error dynamics, transient $\tau$ -tracking	F/T data not required, generalized target $I(s)$ , $\varphi$ -tracking, $\tau$ -tracking, robustness to sys. model uncertainty, opt. feasible $k_D$ region	F/T data not required, $\varphi$ -tracking, $\tau$ -tracking, stability, generalized target $I(s)$

A comparative discussion of different approaches reveals important findings

430 concerning the application of HC, PC, IC, and AC for different purposes. (Implicit) impedance control is the only approach which can be implemented without force information available. It is especially suitable to render low-impedance tracking with high accuracy if a good system model is provided. Admittance control contrarily is not in need of a model and is suitable for tracking high  
435 impedance values. The outer admittance control loop embraces an inner position loop which is a standard feature of industrial robots and equips admittance control with good robustness to disturbances. The control objective of hybrid and parallel force/position control consists in tracking a target force and position instead of a target impedance. Hybrid force/position control divides the  
440 working space of the mechanism in force or position controlled subspaces and hence can only be employed for multi-DOF systems and a detailed environment model available. It is especially effective for high stiffness environments as then in the corresponding subspace pure force control can be applied. Table 11 provides a comparison of the main features, which distinguish these control  
445 concepts, as well as a summary of the potential of their variants to overcome weaknesses of the basic approaches. A comparing simulative case study applied to the same set of system, task and environment models would provide additional insight into their performance and should be considered in future work. Ideally, such a set would span the entire space of application characteristics.  
450 For example, a multi-DOF robotic system operating in a stiff/soft, planar/non-planar, known/uncertain environment with a previously defined/changed task of different complexities might be considered.

Due to the many variants found by the systematic literature research method, the results of Leylavi Shoushtari et al. [31] concerning solutions to the issues of  
455 HC and IC have been extended and furthermore, PC and AC were additionally considered in the analysis. This widens the application limitations of compliant control and the basic approaches and sheds further light on their extended performance capabilities. Due to this and due to the broader definition of compliant control involving PC and HC, this review complements the recent overview of  
460 Calanca et al. [29] on IC and AC of rigid and fixed-compliance systems and

their passivity characteristics.

## 5. Conclusion

This review presents a comprehensive and concise overview of compliant control. Based on a systematic literature analysis, the general design and characteristics as well as variants and combinations of the four main concepts, i.e.,  
465 hybrid and parallel force/position control, impedance and admittance control, are analyzed.

The findings are included in a proposed new scheme to facilitate and systematize the selection process of an appropriate control approach. This scheme  
470 provides valuable assistance particularly to researchers new to the field to navigate through the multitude of different approaches (Figure 4). The scheme guides its user to one of the four main concepts which should be seen as a starting point. Subsequently, Tables 3, 5, 7, 9 and 10 summarize the characteristics of the numerous versions, compound approaches and exceptions of the basic  
475 concepts which are generally targeted to a specialized aim. Thus, they provide support for further adapting the selection of a specific compliant control method to specific needs.

The main contributions of this review are

- (1) a recent review of active compliant control based on an extensive systematic and free literature search providing the reader with the most comprehensive and transparent overview on compliant control that is available  
480 today (Section 2.3),
- (2) a classification of the very many different approaches developed with respect to the four fundamental concepts (Section 3.2 to 3.7),
- (3) a unified and concise summary of the characteristics of these four concepts considering multiple perspectives, and a brief description including  
485 objectives of their different variants, combinations, and non-classifiable exceptions (Section 3.2 to 3.7), and



(4) a novel unified selection scheme to support particularly researchers newly  
490 entering the field in finding and selecting a compliant control approach  
suitable for a given task (Section 3.1).

Apart from variable impedance actuation, continuum and soft material robotics  
are promising future trends to create intrinsic compliance. In such distributed  
systems, blending passive and active compliance to a desired apparent system  
495 compliance poses several new challenges to system dynamics modelling and  
controller design, which may be tackled by optimization [125–127] or learning  
methods. Calanca et al. [29] and Ott [56] give an insight on the influence of fixed  
valued passive compliance in the context of impedance and admittance control.  
Moreover, the increasing system complexity could possibly raise the relevance  
500 of uncertainties and result in increasing robustness requirements. Hence, the  
review on active compliant control provided in this paper also serves as an  
important reference and baseline for the emerging field of distributed compliant  
control where impedance properties are achieved by combinations of passive  
mechatronic hardware design and active digital control concepts.

#### 505 **Acknowledgements**

This work has been partially supported by the German Research Foundation  
(DFG) under grant no. BE 5729/1.

## Appendix

Table A.1 provides a detailed documentation of the systematic literature  
510 search.

Table A.1: Documentation of the systematic literature research

○	Database	Search terms	Results
1	ScienceDirect	force control AND impedance AND KEYWORDS: (control AND review) AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	6+2 <sup>11</sup>
	Web of Science	TOPIC <sup>12</sup> : (force control AND impedance) AND TITLE: (review OR overview) AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	21+2
	IEEEExplore	force control AND (review OR overview) AND AUTHOR KEYWORDS: impedance AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	31+12
	SAGE journals	force control AND (review OR overview) AND KEYWORDS: impedance AND (TIMESPAN(first-2015) OR TIMESPAN(first-2015))	13+17
	WTI Tecfinder	force control AND (review OR overview) AND impedance AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	40+6
	Engineering Village	SUBJECT/TITLE/ABSTRACT: (force control AND (review OR overview) AND impedance) AND CONTROLLED TERM <sup>13</sup> : control AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	37+6
	science.gov	(force control AND (review OR overview) AND impedance AND TIMESPAN(first-2015)) OR ("force control" AND (review OR overview) AND impedance, REFINE: (Topics/Technology/Robotics AND Topics/Research and Development/Robotic AND Topics/Literature Review) AND TIMESPAN(2015-2017))	0+10

<sup>11</sup>The first addend refers to the number of findings for the time span until 2015, the second addend to the number of findings for the time span between 2015 and 2017.

<sup>12</sup>Includes title, abstract, author keywords and keywords plus.

<sup>13</sup>Subject term which describes the content of a document in the most specific and consistent way possible.

Table A.1 (continued): Documentation of the systematic literature research

○ Database	Search terms	Results
2 ScienceDirect	(compliant control AND impedance AND LIMIT-TO (topics, "control") AND LIMIT-TO(topics, "force control, contact, control law, impedance control, contact force, control system") AND TIMESPAN(first-2015)) OR (compliant control AND impedance AND LIMIT-TO (topics, "control") AND LIMIT-TO(topics, "force control, contact, control law, impedance control, control system") AND TIMESPAN(2015-2017))	14+4
Web of Science	compliant control AND impedance AND force AND stiffness AND NOT series elastic actuator AND NOT soft AND NOT adaptive AND (TIMESPAN(1990-2015) OR TIMESPAN(2015-2017))	48+8
IEEEExplore	(METADATA <sup>14</sup> ONLY: (compliant control AND impedance) AND AUTHOR KEYWORDS: control AND TIMESPAN(first-2015)) OR (METADATA ONLY: (compliant control AND impedance AND force AND stiffness) AND AUTHOR KEYWORDS: control AND TIMESPAN(2015-2017))	38+13
SAGE journals	(compliant control AND impedance AND TIMESPAN(first-2015)) OR (compliant control AND impedance AND force AND stiffness AND NOT series elastic actuator AND NOT soft AND TIMESPAN(2015-2017))	31+10
WTI Tecfinder	(compliant control AND impedance AND force AND TIMESPAN(first-2015)) OR (compliant control AND impedance AND force AND stiffness AND TIMESPAN(2015-2017))	37+3
Engineering Village	SUBJECT/TITLE/ABSTRACT: (compliant control AND impedance) AND force AND stiffness AND NOT series elastic actuator AND NOT soft AND NOT adaptive AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	39+13

<sup>14</sup>Includes abstract, index terms and bibliographic citation data (title, publication title, author, etc.).

Table A.1 (continued): Documentation of the systematic literature research

○	Database	Search terms	Results
	science.gov	(compliant control AND impedance AND TIMESPAN(first-2015)) OR ("compliant control" AND impedance AND TIMESPAN(2015-2017))	21+4
3	ScienceDirect	compliant control AND admittance AND LIMIT-TO(topics, "control") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	12+4
	Web of Science	compliant control AND admittance AND force AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	32+9
	IEEEExplore	(METADATA ONLY: (compliant control AND admittance) AND TIMESPAN(first-2015)) OR (METADATA ONLY: (compliant control AND admittance AND force) AND TIMESPAN(2015-2017))	36+9
	SAGE journals	(compliant control AND admittance AND TIMESPAN(first-2015)) OR (compliant control AND admittance AND force AND NOT series elastic actuator AND TIMESPAN(2015-2017))	7+5
	WTI Tecfinder	compliant control AND admittance AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	9+4
	Engineering Village	(SUBJECT/TITLE/ABSTRACT: (compliant control AND admittance) AND TIMESPAN(first-2015)) OR (SUBJECT/TITLE/ABSTRACT: (compliant control AND admittance) AND force AND TIMESPAN(2015-2017))	38+13
	science.gov	(compliant control AND admittance AND TIMESPAN(first-2015)) OR ("compliant control" AND admittance, refine: Topics/Robotic AND TIMESPAN(2015-2017))	4+3
4	ScienceDirect	("human compatible" OR "human compatibility") AND (TITLE-ABSTR-KEY: control OR LIMIT-TO(topics, "human,robot,cognitive architecture") OR (compliance AND LIMIT-TO(topics, "human,contact")) AND TIMESPAN(first-2015)) OR ("human compatible" OR "human compatibility") AND (TITLE-ABSTR-KEY: control OR (compliance AND LIMIT-TO(topics, "human,contact"))) AND TIMESPAN(2015-2017))	45+13

Table A.1 (continued): Documentation of the systematic literature research

○	Database	Search terms	Results
	Web of Science	("human compatible" OR "human compatibility") AND control AND safety AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	4+0
	IEEEExplore	("human compatible" OR "human compatibility") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	11+2
	SAGE journals	("human compatible" OR "human compatibility") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	21+5
	WTI Tecfinder	("human compatible" OR "human compatibility") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	4+2
	Engineering Village	("human compatible" OR "human compatibility") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	43+8
	science.gov	("human compatible control" AND compliance AND TIMESPAN(first-2015)) OR ("human compatible control" AND compliance, REFINE: Topics/Human Factors AND TIMESPAN(2015-2017))	9+0
5	ScienceDirect	TITLE-ABSTR-KEY(active compliance AND control AND force) AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	24+8
	Web of Science	("active compliance" OR "passive compliance") AND control AND force AND (impedance OR admittance) AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	19+5
	IEEEExplore	((("DOCUMENT TITLE": ("active compliance" OR "passive compliance")) OR "ABSTRACT": ("active compliance" OR "passive compliance")) OR "AUTHOR KEYWORDS": ("active compliance" OR "passive compliance")) AND METADATA ONLY: (control AND force) AND SEARCH WITHIN RESULTS: (impedance OR admittance) AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	17+7

Table A.1 (continued): Documentation of the systematic literature research

○ Database	Search terms	Results
SAGE journals	TITLE: ("active compliance" OR "passive compliance") OR ABSTRACT: ("active compliance" OR "passive compliance") OR KEYWORDS: ("active compliance" OR "passive compliance") AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	18+5
WTI Tecfinder	("active compliance" OR "passive compliance") AND control AND "force control" AND (TIMESPAN(first-2015) OR TIMESPAN(2015-2017))	24+1
Engineering Village	(SUBJECT/TITLE/ABSTRACT: ("active compliance" OR "passive compliance") AND control AND force AND (impedance OR admittance) AND TIMESPAN(first-2015)) OR (SUBJECT/TITLE/ABSTRACT: ("active compliance" OR "passive compliance") AND control AND "force control" AND (impedance OR admittance) AND TIMESPAN(2015-2017))	16+6
science.gov	(active compliance AND control AND force AND TIMESPAN(first-2015)) OR ("active compliance" AND control AND force, REFINE: (Topics/Control System/Control Strategy AND Topics/Robotic AND Topics/Human Factors) AND TIMESPAN(2015-2017))	36+8
<b>Total results:</b>		<b>1032</b>

## References

- [1] S. Wolf, G. Grioli, O. Eiberger, W. Friedl, M. Grebenstein, H. Hoppner, E. Burdet, D. G. Caldwell, R. Carloni, M. G. Catalano, D. Lefeber, S. Stramigioli, N. Tsagarakis, M. Van Damme, R. Van Ham, B. Vanderborght, L. C. Visser, A. Bicchi, A. Albu-Schäffer, Variable Stiffness Actuators: Review on Design and Components, *IEEE/ASME Transactions on Mechatronics* 21 (5) (2016) 2418–2430.

- 520 [2] P. Beckerle, J. Wojtusich, S. Rinderknecht, O. von Stryk, Analysis of System Dynamic Influences in Robotic Actuators with Variable Stiffness, *Smart Structures and Systems* 13 (4) (2014) 711–730.
- 525 [3] B. Vanderborght, A. Albu-Schaeffer, A. Bicchi, E. Burdet, D. G. Caldwell, R. Carloni, M. G. Catalano, O. Eiberger, W. Friedl, G. Ganesh, M. Garabini, M. Grebenstein, G. Grioli, S. Haddadin, H. Hoppner, A. H. Jafari, M. Laffranchi, D. Lefeber, F. Petit, S. Stramigioli, N. Tsagarakis, M. Van Damme, R. Van Ham, L. C. Visser, S. Wolf, Variable impedance actuators: A review, *Robotics and Autonomous Systems* 61 (12) (2013) 1601–1614.
- 530 [4] R. Van Ham, T. Sugar, B. Vanderborght, K. W. Hollander, D. Lefeber, Compliant Actuator Designs, *IEEE Robotics & Automation Magazine* 16 (3) (2009) 81–94.
- 535 [5] T. Tang, H.-C. Lin, Y. Zhao, Y. Fan, W. Chen, M. Tomizuka, Teach Industrial Robots Peg-Hole-Insertion by Human Demonstration, in: *IEEE International Conference on Advanced Intelligent Mechatronics*, Banff, Canada, 2016, pp. 488–494.
- [6] F. Dimeas, N. Aspragathos, Online Stability in Human-Robot Cooperation with Admittance Control, *IEEE Transactions on Haptics* 9 (2) (2016) 267–278.
- 540 [7] R. Riener, L. Lünenburger, I. C. Maier, G. Colombo, V. Dietz, Locomotor Training in Subjects with Sensori-Motor Deficits: An Overview of the Robotic Gait Orthosis Lokomat, *Journal of Healthcare Engineering* 1 (2) (2010) 197–216.
- 545 [8] M. Sharifi, S. Behzadipour, H. Salarieh, Nonlinear Bilateral Adaptive Impedance Control With Applications in Telesurgery and Telerehabilitation, *Journal of Dynamic Systems, Measurement, and Control* 138 (11) (2016) 1–16.
- 550 [9] B. Ugurlu, I. Havoutis, C. Semini, K. Kayamori, D. G. Caldwell, T. Narikiyo, Pattern generation and compliant feedback control for quadrupedal dynamic trot-walking locomotion: experiments on RoboCat-1 and HyQ, *Autonomous Robots* 38 (4) (2015) 415–437.
- [10] Franka Emika GmbH, Panda Datasheet (2018).
- [11] KUKA AG, Sensitive robotics LBR iiwa (2017).

- [12] M. Zinn, O. Khatib, B. Roth, J. K. Salisbury, Playing It Safe, *IEEE Robotics & Automation Magazine* 11 (2) (2004) 12–21.
- 555 [13] A. Bicchi, G. Tonietti, Fast and "soft-arm" tactics, *IEEE Robotics and Automation Magazine* 11 (2) (2004) 22–33.
- [14] S. Haddadin, A. Albu-Schäffer, O. Eiberger, G. Hirzinger, New insights concerning intrinsic joint elasticity for safety, in: *IEEE/RSJ International Conference on Intelligent Robots and Systems*, Taipei, Taiwan, 2010, pp. 2181–2187.
- 560 [15] T. Lens, J. Kunz, C. Trommer, A. Karguth, O. von Stryk, BioRob-Arm: A Quickly Deployable and Intrinsically Safe , Light-Weight Robot Arm for Service Robotics Applications, in: *International Symposium on Robotics/German Conference on Robotics*, 2010, pp. 905–910.
- 565 [16] T. Lens, Physical Human-Robot Interaction with a Lightweight, Elastic Tendon Driven Robotic Arm: Modeling, Control, and Safety Analysis, Phd thesis, TU Darmstadt (2012).
- [17] G. Zeng, A. Hemami, An overview of robot force control, *Robotica* 15 (5) (1997) 473–482.
- 570 [18] M. K. Vukobratović, D. T. Surdilovic, Control of Robotic Systems in Contact Tasks: An Overview, *Journal of Computer and Systems Sciences International* 36 (5) (1997) 817–836.
- [19] J. C. Grieco, G. Fernandez, M. Armada, P. González-de Santos, A Review on Force Control of Robot Manipulators, *Studies in Informatics and Control* 3 (2) (1994) 241–252.
- 575 [20] T. Yoshikawa, Force Control of Robot Manipulators, in: *Proceedings of the IEEE International Conference on Robotics & Automation*, 2000, pp. 220–226.
- [21] S. Chiaverini, B. Siciliano, L. Villani, A Survey of Robot Interaction Control Schemes with Experimental Comparison, *IEEE/ASME Transactions on Mechatronics* 4 (3) (1999) 273–285.
- 580 [22] T. Lefebvre, J. Xiao, H. Bruyninckx, G. De Gerssem, Active Compliant Motion: A Survey, *Advanced Robotics* 19 (5) (2005) 479–499.



- 585 [23] W. Khalil, E. Dombre, Compliant motion control, in: Modeling, Identification and Control of Robots, Kogan Page Science, London, 2004, Ch. 15, pp. 377–393.
- [24] S. G. Khan, G. Herrmann, M. Al Grafi, T. Pipe, C. Melhuish, Compliance Control and Human-Robot Interaction: Part 1 - Survey, *International Journal of Humanoid Robotics* 11 (3) (2014) 1–28.
- 590 [25] M. Vukobratović, A. Tuneski, Contact Control Concepts in Manipulation Robotics - An Overview, *IEEE Transactions on Industrial Electronics* 41 (1) (1994) 12–24.
- [26] L. Villani, J. De Schutter, Force Control, in: B. Siciliano, O. Khatib (Eds.), *Handbook of Robotics*, 1st Edition, Springer, Berlin; Heidelberg, 2008, Ch. 7, pp. 161–185.
- 595 [27] J. De Schutter, H. Bruyninckx, W.-H. Zhu, M. W. Spong, Force control: a bird’s eye view, in: B. Siciliano, K. P. Valavanis (Eds.), *Control Problems in Robotics and Automation. Lecture Notes in Control and Information Sciences*, Vol. 230, Springer, Berlin; Heidelberg, 1998, pp. 1–14.
- [28] M. Vukobratović, D. Surdilovic, Y. Ekalo, D. Katic, *Dynamics and Robust Control of Robot-Environment Interaction*, World Scientific, Singapore, 2009.
- 600 [29] A. Calanca, R. Muradore, P. Fiorini, A Review of Algorithms for Compliant Control of Stiff and Fixed-Compliance Robots, *IEEE/ASME Transactions on Mechatronics* 21 (2) (2016) 613–624.
- 605 [30] S. Flixeder, T. Glück, A. Kugi, Modeling and Force Control for the Collaborative Manipulation of Deformable Strip-Like Materials, *IFAC-PapersOnLine* 49 (21) (2016) 95–102.
- [31] A. Leylavi Shoushtari, P. Dario, S. Mazzoleni, A review on the evolvement trend of robotic interaction control, *Industrial Robot: An International Journal* 43 (5) (2016) 535–551.
- 610 [32] S. P. Patarinski, R. G. Botev, Robot Force Control: A Review, *Mechatronics* 3 (4) (1993) 377–398.
- [33] A. Calanca, *Compliant Control of Elastic Actuators for Human Robot Interaction*, Thesis, University of Verona (2014).
- 615

- [34] N. Hogan, Impedance Control: An Approach to Manipulation, *Journal of Dynamic Systems, Measurement, and Control* 107 (1) (1985) 1–24.
- [35] T. Nef, P. Lum, Improving backdrivability in geared rehabilitation robots, *Medical & Biological Engineering & Computing* 47 (4) (2009) 441–447.
- 620 [36] W. T. Townsend, The Effect of Transmission Design on Force-Controlled Manipulator Performance, Ph.D. thesis, Massachusetts Institut of Technology (1988).
- [37] D. M. Gorinevsky, A. M. Formalsky, A. Y. Schneider, *Force Control of Robotics Systems*, CRC Press, Boca Raton, 1997.
- 625 [38] P. Weiss, P. Zenker, E. Maehle, Feed-forward Friction and Inertia Compensation for Improving Backdrivability of Motors, in: *International Conference on Control, Automation, Robotics & Vision*, 2012, pp. 288–293.
- [39] M.-W. Ueberle, Design, Control, and Evaluation of a Family of Kinesthetic Haptic Interfaces, Ph.D. thesis, Technical University of Munich (2006).
- 630 [40] H. Kazerooni, P. Houpt, T. Sheridan, The fundamental concepts of robust compliant motion for robot manipulators, in: *IEEE International Conference on Robotics and Automation*, Vol. 3, 1986, pp. 418–427.
- [41] B. Siciliano, L. Villani, *Robot Force Control*, 1st Edition, Vol. 540 of The Kluwer International Series in Engineering and Computer Science, Kluwer Academic Publishers, Norwell, MA, USA, 1999.
- 635 [42] D. J. Latornell, D. B. Cherechas, Force and Motion Control of a Single Flexible Manipulator Link, *Robotics and Computer-Integrated Manufacturing* 9 (2) (1992) 87–99.
- [43] M. Vukobratović, How to Control Robots Interacting with Dynamic Environment, *Journal of Intelligent and Robotic Systems* 19 (2) (1997) 119–152.
- 640 [44] M. H. Raibert, J. J. Craig, Hybrid Position/Force Control of Manipulators, *Journal of Dynamic Systems, Measurement, and Control* 103 (2) (1981) 126–133.
- 645 [45] S. Chiaverini, L. Sciavicco, The Parallel Approach to Force/Position Control of Robotic Manipulators, *IEEE Transactions on Robotics and Automation* 9 (4) (1993) 361–373.

- [46] M. T. Mason, Compliance and Force Control for Computer Controlled Manipulators, *IEEE Transactions on Systems, Man and Cybernetics* 11 (6) (1981) 418–432.
- 650
- [47] C. H. An, J. M. Hollerbach, The Role of Dynamic Models in Cartesian Force Control of Manipulators, *The International Journal of Robotics Research* 8 (4) (1989) 51–72.
- [48] Y. Yoshida, A. Yabuki, Y. Nakata, K. Nishimoto, High-Speed Force Controller for SCARA Robots, in: *Annual Conference of IEEE Industrial Electronics Society*, Philadelphia, USA, 1989, pp. 629–633.
- 655
- [49] L. Villani, C. Canudas De Wit, B. Brogliato, An Exponentially Stable Adaptive Control for Force and Position Tracking of Robot Manipulators, *IEEE Transactions on Automatic Control* 44 (4) (1999) 798–802.
- [50] B. Siciliano, L. Villani, A Passivity-based Approach to Force Regulation and Motion Control of Robot Manipulators, *Automatica* 32 (3) (1996) 443–447.
- 660
- [51] S. Chiaverini, L. Sciavicco, Force/Position Control of Manipulators in Task Space with Dominance in Force, *IFAC Proceedings Volumes* 21 (16) (1988) 137–143.
- 665
- [52] B. Siciliano, L. Villani, A Passivity-Based Force/Position Control Scheme for Robot Manipulators, in: *IEEE International Conference on Robotics and Automation*, San Diego, USA, 1994, pp. 3265–3270.
- [53] C. C. Chen, J. S. Li, J. Luo, S. R. Xie, H. Y. Li, H. Y. Pu, J. Gu, Robust Adaptive Position and Force Tracking Control Strategy for Door-Opening Behaviour, *International Journal of Simulation Modelling* 15 (3) (2016) 423–435.
- 670
- [54] F. Caccavale, P. Chiacchio, S. Chiaverini, Task-space regulation of cooperative manipulators, *Automatica* 36 (6) (2000) 879–887.
- [55] P. Hsu, Coordinated Control of Multiple Manipulator Systems, *IEEE Transactions on Robotics and Automation* 9 (4) (1993) 400–410.
- 675
- [56] C. Ott, Cartesian Impedance Control of Redundant and Flexible-Joint Robots, in: B. Siciliano, O. Khatib, F. Groen (Eds.), *Springer Tracts in Advanced Robotics*, Vol. 49, Springer, Berlin; Heidelberg, 2008.

- 680 [57] H. Zhuang, H. Gao, Z. Deng, L. Ding, Z. Liu, A review of heavy-duty legged robots, *Science China Technological Sciences* 57 (2) (2014) 298–314.
- [58] A. Lopes, F. Almeida, A force-impedance controlled industrial robot using an active robotic auxiliary device, *Robotics and Computer-Integrated Manufacturing* 24 (3) (2008) 299–309.
- 685 [59] A. Albu-Schäffer, G. Hirzinger, Cartesian Impedance Control Techniques for Torque Controlled Light-Weight Robots, in: *IEEE International Conference on Robotics & Automation*, Washington, USA, 2002, pp. 657–663.
- [60] T. Valency, M. Zacksenhouse, Accuracy/Robustness Dilemma in Impedance Control, *Journal of Dynamic Systems, Measurement, and Control* 125 (3) (2003) 310–319.
- 690 [61] T. Boaventura, G. A. Medrano-Cerda, C. Semini, J. Buchli, D. G. Caldwell, Stability and Performance of the Compliance Controller of the Quadruped Robot HyQ, in: *IEEE/RSJ International Conference on Intelligent Robots and Systems*, Tokyo, Japan, 2013, pp. 1458–1464.
- 695 [62] M. Tufail, C. W. de Silva, Impedance Control Schemes for Bilateral Teleoperation, in: *International Conference on Computer Science & Education*, Vancouver, Canada, 2014, pp. 44–49.
- [63] A. Ajoudani, N. G. Tsagarakis, A. Bicchi, Choosing Poses for Force and Stiffness Control, *IEEE Transactions on Robotics* 33 (6) (2017) 1483 – 1490.
- 700 [64] M. Mendoza-Gutierrez, F. Reyes, I. Bonilla-Gutierrez, E. Gonzalez-Galvan, Proportional-derivative impedance control of robot manipulators for interaction tasks, *Proceedings of the Institution of Mechanical Engineers, Part I: Journal of Systems and Control Engineering* 225 (3) (2011) 315–329.
- 705 [65] R. A. Volpe, Real and Artificial Forces in the Control of Manipulators: Theory and Experiments, Ph.D. thesis, Carnegie Mellon University (1990).
- 710 [66] S. A. A. Moosavian, E. Papadopoulos, Cooperative Object Manipulation with Contact Impact Using Multiple Impedance Control, *International Journal of Control, Automation and, Systems* 8 (2) (2010) 314–327.

- 715 [67] S. A. Schneider, R. H. Cannon, Object Impedance Control for Cooperative Manipulation - Theory and Experimental Results, *IEEE Transactions on Robotics and Automation* 8 (3) (1992) 383–394.
- [68] R. G. Bonitz, T. C. Hsia, Internal Force-Based Impedance Control for Cooperating Manipulators, *IEEE Transactions on Robotics and Automation* 12 (1) (1996) 78–89.
- 720 [69] F. Caccavale, P. Chiacchio, A. Marino, L. Villani, Six-DOF Impedance Control of Dual-Arm Cooperative Manipulators, *IEEE/ASME Transactions on Mechatronics* 13 (5) (2008) 576–586.
- [70] R. Volpe, P. Khosla, The Equivalence of Second-Order Impedance Control and Proportional Gain Explicit Force Control, *The International Journal of Robotics Research* 14 (6) (1995) 574–589.
- 725 [71] J. K. Salisbury, Active Stiffness Control of a Manipulator in Cartesian Coordinates, in: *IEEE Conference on Decision and Control including the Symposium on Adaptive Processes*, Albuquerque, USA, 1980, pp. 95–100.
- [72] R. J. Anderson, Dynamic Damping Control: Implementation Issues and Simulation Results, in: *IEEE International Conference on Robotics and Automation*, Cincinnati, USA, 1990, pp. 68–77.
- 730 [73] A. Jain, M. D. Killpack, A. Edsinger, C. C. Kemp, Reaching in clutter with whole-arm tactile sensing, *The International Journal of Robotics Research* 32 (4) (2013) 458–482.
- [74] Q. Xu, Robust Impedance Control of a Compliant Microgripper for High-Speed Position/Force Regulation, *IEEE Transactions on Industrial Electronics* 62 (2) (2015) 1201–1209.
- 735 [75] R. Volpe, P. Khosla, Computational Considerations in the Implementation of Force Control Strategies, *Journal of Intelligent & Robotic Systems* 9 (1-2) (1994) 121–148.
- 740 [76] H. Sadeghian, L. Villani, M. Keshmiri, B. Siciliano, Task-Space Control of Robot Manipulators With Null-Space Compliance, *IEEE Transactions on Robotics* 30 (2) (2014) 493–506.
- [77] H. Chen, Y. Liu, Robotic assembly automation using robust compliant control, *Robotics and Computer-Integrated Manufacturing* 29 (2) (2013) 293–300.
- 745

- [78] H. C. Liaw, B. Shirinzadeh, Robust generalised impedance control of piezo-actuated flexure-based four-bar mechanisms for micro/nano manipulation, *Sensors and Actuators* 148 (2) (2008) 443–453.
- [79] J. Pratt, C. M. Chew, A. Torres, P. Dilworth, G. Pratt, Virtual Model Control: An Intuitive Approach for Bipedal Locomotion, *The International Journal of Robotics Research* 20 (2) (2001) 129–143.
- [80] H. Maass, B. B. A. Chantier, H. K. Cakmak, C. Trantakis, U. G. Kuehnappel, Fundamentals of Force Feedback and Application to a Surgery Simulator, *Computer Aided Surgery* 8 (6) (2003) 283–291.
- [81] C. Chávez-Olivares, F. Reyes-Cortés, E. González-Galván, On Stiffness Regulators with Dissipative Injection for Robot Manipulators, *International Journal of Advanced Robotic Systems* 12 (6) (2015) 1–15.
- [82] S. Choudhary, N. K. Jha, Intelligent Automation of Industrial Machines, in: *International Conference on Industrial Electronics, Control, and Instrumentation*, Maui, USA, 1993, pp. 475–480.
- [83] P. Agarwal, A. D. Deshpande, Impedance and Force-field Control of the Index Finger Module of a Hand Exoskeleton for Rehabilitation, in: *IEEE International Conference on Rehabilitation Robotics*, Singapore, Singapore, 2015, pp. 85–90.
- [84] S. Jung, T. C. Hsia, R. G. Bonitz, Force Tracking Impedance Control for Robot Manipulators with an Unknown Environment: Theory, Simulation and Experiment, *The International Journal of Robotics Research* 20 (9) (2001) 765–774.
- [85] L. Roveda, F. Vicentini, N. Pedrocchi, F. Braghin, L. Molinari Tosatti, Impedance Shaping Controller for Robotic Applications Involving Interacting Compliant Environments and Compliant Robot Bases, in: *IEEE International Conference on Robotics and Automation*, Seattle, USA, 2015, pp. 2066–2071.
- [86] L. Roveda, F. Vicentini, N. Pedrocchi, L. Molinari Tosatti, Impedance Control based Force-tracking Algorithm for Interaction Robotics Tasks: An Analytically Force Overshoots-free Approach, in: *International Conference on Informatics in Control, Automation and Robotics*, Colmar, France, 2015, pp. 386–391.

- 780 [87] L. Roveda, N. Pedrocchi, F. Vicentini, L. Molinari Tosatti, An interaction  
controller formulation to systematically avoid force overshoots through  
impedance shaping method with compliant robot base, *Mechatronics* 39  
(2016) 42–53.
- [88] L. Roveda, N. Pedrocchi, F. Vicentini, L. Molinari Tosatti, Industrial  
Compliant Robot Bases in Interaction Tasks: A force Tracking Algorithm  
785 with Coupled Dynamics Compensation, *Robotica* 35 (8) (2017) 1732–  
1746.
- [89] Q. P. Ha, Q. H. Nguyen, D. C. Rye, H. F. Durrant-Whyte, Impedance control  
of a hydraulically-actuated robotic excavator, *Journal of Automation  
in Construction* 9 (5-6) (2000) 421–435.
- 790 [90] M. Jin, S. H. Kang, P. H. Chang, Robust Compliant Motion Control of  
Robot Manipulators with Nonlinear Friction Using Time Delay Estima-  
tion, *IEEE Transactions on Industrial Electronics* 55 (1) (2008) 258–269.
- [91] P. H. Chang, M. Jin, Nonlinear Target Impedance Design and Its Use  
in Robot Compliant Motion Control with Time Delay Estimation, in:  
795 Annual Conference of IEEE Industrial Electronics, Paris, France, 2006,  
pp. 161–166.
- [92] P. H. Chang, K. Park, S. H. Kang, H. I. Krebs, N. Hogan, Stochastic Esti-  
mation of Human Arm Impedance Using Robots With Nonlinear Frictions:  
An Experimental Validation, *IEEE/ASME Transactions on Mechatronics*  
800 18 (2) (2013) 775–786.
- [93] S. H. Kang, M. Jin, P. H. Chang, An IMC Based Enhancement of Accu-  
racy and Robustness of Impedance Control, in: *IEEE International Con-  
ference on Robotics and Automation*, Pasadena, USA, 2008, pp. 2623–  
2628.
- 805 [94] R. Volpe, P. Khosla, A Theoretical and Experimental Investigation of  
Explicit Force Control Strategies for Manipulators, *IEEE Transactions on  
Automatic Control* 38 (11) (1993) 1634–1650.
- [95] D. Kaserer, H. Gatringer, A. Müller, Admittance control of a redundant  
industrial manipulator without using force/torque sensors, in: *Annual  
810 Conference of the IEEE Industrial Electronics Society*, Florence, Italy,  
2016, pp. 5310–5315.

- [96] S. S. Ge, Y. Li, C. Wang, Impedance adaptation for optimal robot-environment interaction, *International Journal of Control* 87 (2) (2014) 249–263.
- 815 [97] Y. Li, S. S. Ge, Impedance Learning for Robots Interacting with Unknown Environments, *IEEE Transactions on Control Systems Technology* 22 (4) (2014) 1422–1432.
- [98] L. Santos, R. Cortesão, Admittance Control for Robotic-Assisted Tele-Echography, in: *International Conference on Advanced Robotics*, Montevideo, Uruguay, 2013, pp. 1–7.
- 820 [99] F. Caccavale, C. Natale, B. Siciliano, L. Villani, Integration for the Next Generation: Embedding Force Control into Industrial Robots, *IEEE Robotics & Automation Magazine* 12 (3) (2005) 53–64.
- [100] Y. Chen, J. Hu, W. Wang, L. Peng, L. Peng, Z.-G. Hou, An FES-assisted Training Strategy Combined with Impedance Control for a Lower Limb Rehabilitation Robot, in: *IEEE International Conference on Robotics and Biomimetics*, Shenzhen, China, 2013, pp. 2037–2042.
- 825 [101] A. Denève, S. Moughamir, L. Afilal, J. Zaytoon, Control system design of a 3-DOF upper limbs rehabilitation robot, *Computer Methods and Programs in Biomedicine* 89 (2) (2008) 202–214.
- 830 [102] A. Atawnih, D. Papageorgiou, Z. Doulgeri, Reaching for redundant arms with human-like motion and compliance properties, *Robotics and Autonomous Systems* 62 (12) (2014) 1731–1741.
- [103] H. Kazerooni, Direct-Drive Active Compliant End Effector (Active RCC), *IEEE Journal on Robotics and Automation* 4 (3) (1988) 324–333.
- 835 [104] D. E. Whitney, Historical Perspective and State of the Art in Robot Force Control, *The International Journal of Robotics Research* 6 (1) (1987) 3–14.
- [105] D. E. Whitney, Force Feedback Control of Manipulator Fine Motions, *Journal of Dynamic Systems, Measurement, and Control* 99 (2) (1977) 91–97.
- 840 [106] C. Zhou, Z. Li, J. Castano, H. Dallali, N. G. Tsagarakis, D. G. Caldwell, A passivity based compliance stabilizer for humanoid robots, in: *IEEE International Conference on Robotics & Automation*, Hong Kong, China, 2014, pp. 1487–1492.
- 845



- [107] S. Oh, H. Woo, K. Kong, Frequency-Shaped Impedance Control for Safe Human Robot Interaction in, *IEEE/ASME Transactions on Mechatronics* 19 (6) (2014) 1907–1916.
- [108] Y. Xie, D. Sun, C. Liu, H. Y. Tse, S. H. Cheng, A Force Control Approach to a Robot-assisted Cell Microinjection System, *International Journal of Robotics Research* 29 (9) (2010) 1222–1232.
- [109] J. Bös, A. Wahrburg, K. D. Listmann, Iteratively Learned and Temporally Scaled Force Control with Application to Robotic Assembly in Unstructured Environments, in: *IEEE International Conference on Robotics and Automation*, Singapore, Singapore, 2017, pp. 3000–3007.
- [110] G. D. Glosser, W. S. Newman, The Implementation of a Natural Admittance Controller on an Industrial Manipulator, in: *IEEE International Conference on Robotics and Automation*, San Diego, USA, 1994, pp. 1209–1215.
- [111] D. J. Buckmaster, W. S. Newman, S. D. Somes, Compliant Motion Control for Robust Robotic Surface Finishing, in: *World Congress on Intelligent Control and Automation*, Chongqing, China, 2008, pp. 559–564.
- [112] X. Xiong, F. Wörgötter, P. Manoonpong, Adaptive and Energy Efficient Walking in a Hexapod Robot Under Neuromechanical Control and Sensorimotor Learning, *IEEE Transactions on Cybernetics* 46 (11) (2016) 2521–2534.
- [113] S. Tauscher, A. Fuchs, F. Baier, L. A. Kahrs, T. Ortmaier, High-accuracy drilling with an image guided light weight robot: autonomous versus intuitive feed control, *International Journal of Computer Assisted Radiology and Surgery* 12 (10) (2017) 1763–1773.
- [114] P. Marayong, M. Li, A. M. Okamura, G. D. Hager, Spatial Motion Constraints: Theory and Demonstrations for Robot Guidance Using Virtual Fixtures, in: *IEEE International Conference on Robotics and Automation*, Tapei, Taiwan, 2003, pp. 1954–1959.
- [115] R. J. Anderson, M. W. Spong, Hybrid Impedance Control of Robotic Manipulators, *IEEE Journal on Robotics and Automation* 4 (5) (1988) 549–556.

- [116] F. Shadpey, R. V. Patel, C. Balafoutis, C. Tessier, Compliant Motion Control and Redundancy Resolution for Kinematically Redundant Manipulators, in: American Control Conference, Washington DC, USA, 1995, pp. 392–396.
- [117] A. Gonzales Marin, R. Weitschat, Unified Impedance and Hybrid Force-Position Controller with Kinestatic Filtering, in: IEEE/RSJ International Conference on Intelligent Robots and Systems, Daejeon, Korea, 2016, pp. 3353–3359.
- [118] H. Montes, M. Armada, Force Control Strategies in Hydraulically Actuated Legged Robots, *International Journal of Advanced Robotic Systems* 13 (2) (2016) 1–16.
- [119] C. Ott, R. Mukherjee, Y. Nakamura, Unified Impedance and Admittance Control, in: IEEE International Conference on Robotics and Automation, Anchorage, Alaska, 2010, pp. 554–561.
- [120] N. Mol, J. Smisek, R. Babuška, A. Schiele, Nested compliant admittance control for robotic mechanical assembly of misaligned and tightly tolerated parts, in: IEEE International Conference on Systems, Man, and Cybernetics, Budapest, Hungary, 2016, pp. 2717–2722.
- [121] A. Dietrich, K. Bussmann, F. Petit, P. Kotyczka, C. Ott, B. Lohmann, A. Albu-Schäffer, Whole-body impedance control of wheeled mobile manipulators, *Autonomous Robots* 40 (3) (2016) 505–517.
- [122] R. Volpe, P. Khosla, Experimental Verification of a Strategy for Impact Control, in: IEEE International Conference on Robotics and Automation, Sacramento, USA, 1991, pp. 1854–1860.
- [123] S. M. Prabhu, D. P. Garg, Fuzzy Reinforcement Compliance Control for Robotic Assembly, in: IEEE International Symposium on Intelligent Control, Monterey, USA, 1995, pp. 623–628.
- [124] F. J. Abu-Dakka, B. Nemeč, J. A. Jørgensen, T. R. Savarimuthu, N. Krüger, A. Ude, Adaptation of manipulation skills in physical contact with the environment to reference force profiles, *Autonomous Robots* 39 (2) (2015) 199–217.
- [125] M. Garabini, A. Passaglia, F. Belo, P. Salaris, A. Bicchi, Optimality Principles in Stiffness Control : The VSA Kick, in: IEEE International Conference on Robotics and Automation, 2012.

- [126] F. Petit, A. Albu-Schaeffer, Cartesian Impedance Control for a Variable Stiffness Robot Arm, in: IEEE/RSJ International Conference on Intelligent Robots and Systems, 2011, pp. 4180–4186.
- <sup>915</sup> [127] D. Braun, M. Howard, S. Vijayakumar, Optimal variable stiffness control: Formulation and application to explosive movement tasks, *Autonomous Robots* 33 (3) (2012) 237–253.